













## Epidemiologic Measures: How we combine numbers

Rate	$r = \frac{\Delta x}{\Delta t}$	Change in x per change in t
Proportion	$p = \frac{a}{a+b}$	Numerator is part of the denominator
	$P = \left( \frac{a}{a+b} \right) \times 100$	Percent
Ratio	$R = \frac{x}{y}$	x and y are different and are compared

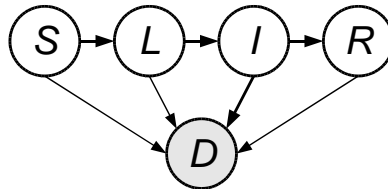
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Notes:

## Epidemiologic Measures: Measures of occurrence

- Count
- Time
- Rate
- Risk or Odds
- Prevalence



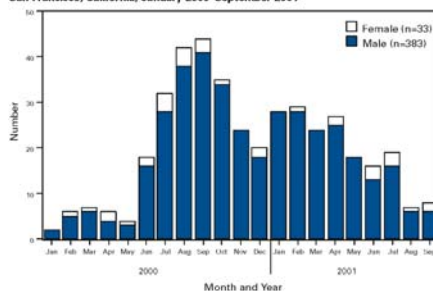
S = Susceptible  
L = Latent infection  
I = Infective  
R = Recovered  
D = Dead

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## Community outbreak of shigellosis, San Francisco, 2000

FIGURE 1. Number of adult *Shigella sonnei* infections, by month, year, and sex — San Francisco, California, January 2000–September 2001



During June–December 2000, 230 cases of culture-confirmed\* *S. sonnei* infection were reported to the San Francisco Department of Public Health; an average of 21 cases (range: 13–29 cases) occurred during the same period from 1996 to 1999. [MMWR 2004;50(42):922]

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\*Residents of San Francisco County aged  $\geq 15$  years.

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## Epidemiologic Measures: Measures of occurrence - Rate

$$\text{rate} = \frac{\text{Number of events}}{\text{Person-time at risk}}$$

$$\text{Period rate}_{1989-1991} = \frac{D_{1989} + D_{1990} + D_{1991}}{K_{1989} + K_{1990} + K_{1991}}$$

$D_x$  = Events in year  $x$

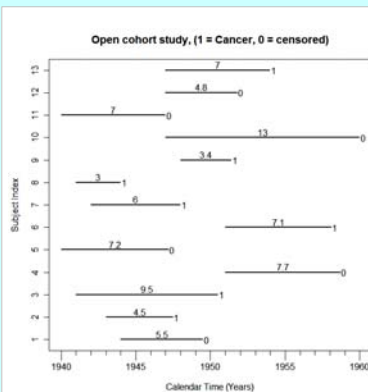
$K_x$  = Midyear population estimate in year  $x$

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Notes:

## Measures of occurrence – Cancer rates in an open cohort study, Person-time data



$$\begin{aligned} \text{rate} &= \frac{\# \text{cases}}{\sum \text{person-time}_i} \\ &= \frac{7 \text{ cases}}{85.7 \text{ person-years}} \\ &= 0.08168028 \\ &= 8.2 \text{ cases per } 100 \text{ py} \end{aligned}$$

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## Measures of occurrence - Period rates: Female breast cancer deaths, San Francisco

### Annual period rates

CATEGORIES	YEAR		
	1989	1990	1991
Breast cancer deaths	125	130	131
Female population	361,975	361,401	366,613
Rate per 100,000 per year	34.5	36.0	35.7

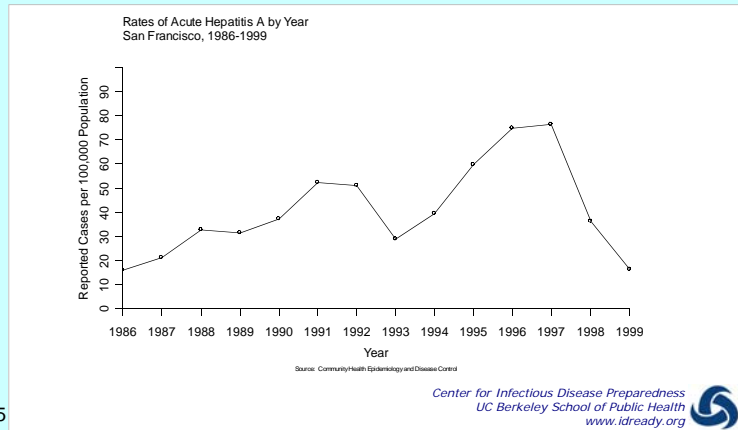
### Period rates

$$\begin{aligned} r_{1989-1991} &= \frac{125 + 130 + 131}{361,975 + 361,401 + 366,613} \\ &= 35.4 \text{ per } 100,000 \text{ per year} \end{aligned}$$

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## Rates of acute hepatitis A, San Francisco, 1986-1999



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Notes:

## Epidemiologic Measures: Measures of occurrence - Risk

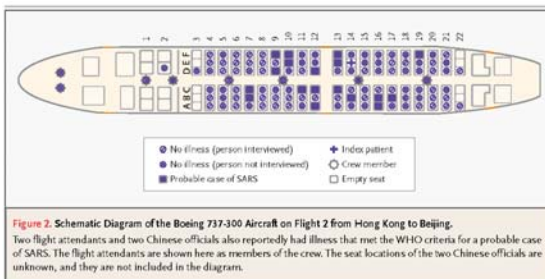
- Risk is a probability
- Probability models used to calculate risk
  - Binomial model (our focus)
  - Hazard-based models (not today)
    - Constant hazard (constant rate) model
    - Non-constant hazard model
      - Exponential formula method (fixed time intervals)
      - Kaplan-Meier method (time-to-event data)

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## Measures of occurrence – Risk estimation with binomial data

$$R(0,t) = \frac{\# \text{events in } (0,t)}{\text{Population at risk at time } 0} = \frac{18}{111} = 0.1622$$



NEJM 2003, 349;25:2416

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Notes:

## Outbreak of nodding off at CIDP lectures: Risk ratio & Odds ratio

	Exposure	
	Tomás	Other
Individuals nodding off	19	12
Cases of any nodding off	21	13
Number started conference	100	100

$$R_1 = \frac{19}{100} = 0.19$$

$$R_0 = \frac{12}{100} = 0.12$$

Why is this analytic approach not recommended?

$$RR = \frac{R_1}{R_0} = 1.58$$

$$OR = \frac{R_1/(1-R_1)}{R_0/(1-R_0)} = 1.72$$

$p$  value = 0.24

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## Outbreak of nodding off at CIDP lectures: Risk ratio & Odds ratio

	Exposure	
	Tomás	Other
Cases of nodding off	21	13
No. started lecture	559	1151

$$R_1 = \frac{21}{559} = 0.0376$$

$$R_0 = \frac{13}{1151} = 0.0113$$

$$RR = \frac{R_1}{R_0} = 3.33$$

$$OR = \frac{R_1/(1-R_1)}{R_0/(1-R_0)} = 3.42$$

$p$  value = 0.0006

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## Outbreak of nodding off at CIDP lectures: Rate ratio

	Exposure	
	Tomás	Other
Cases of nodding off	21	13
Person-hours at lecture	522.7	1047.3

$$r_1 = \frac{21}{522.7} = 0.0402$$

$$r_0 = \frac{13}{1047.3} = 0.0124$$

$$rr = \frac{r_1}{r_0} = 3.24$$

$p$  value = 0.0008

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